### Metaheuristic algorithms.

# Lab 4: Evolution strategies. Genetic programming.

### **1. Evolution Strategies**

Evolution strategies are mainly used to solve continuous optimization problems. In the case of evolution strategies, the elements of the population are real vectors and the main components are:

- Selection: it is used only to select the survivors (all elements can be parents) and it is usually a deterministic selection based on taking the best M offsprings from the set of L offsprings (in the case of (M,L) strategies) or the best M elements from the joined population of parents and offsprings (in the case of (M+L) variants). M denotes the number of elements in the current population and L denotes the number of elements generated using recombination and mutation.
- *Recombination:* from R parents is constructed one offspring by linear (convex) combination. For a population of M elements are constructed through recombination M new elements which are further modified by applying mutation.
- *Mutation:* it is applied to all elements in the population and consists of adding a random value (generated according to a given distribution).

**Application 1.** Implement a simple evolution strategy having the following characteristics:

- Convex recombination (an offspring is computed as the average of R parents the number of parents is an input parameter)
- Mutation based on additive random perturbation relying on random values generated according to a normal distribution (N(0,sigma) = 0 mean, standard deviation equal to sigma; sigma is an input parameter)
- Selection of survivors: M+L variant based on truncation or tournament strategy.

Test functions:

See for instance: http://www-optima.amp.i.kyotou.ac.jp/member/student/hedar/Hedar\_files/TestGO\_files/Page364.htm

*Hint:* an example is implemented in SE.sci

#### **Exercises:**

- 1. Test SE.sci for sphere, Griewank, Ackley, Rastrigin and Rosenbrock functions described in the web page <u>http://www-optima.amp.i.kyoto-</u> <u>u.ac.jp/member/student/hedar/Hedar files/TestGO files/Page364.htm</u>
- 2. Analyze the impact of the parameter sigma on the ES performance by using values smaller and larger than 1.
- 3. Analyze the impact of the selection type ((M+L) vs. (M,L), truncation vs tournamet) on the ES performance.

# **Application 2.**

Analyse the behaviour of the Covariance Matrix Adaptation algorithm (CMA-ES) in the case of nonseparable objective functions (the variables are correlated).

*Hint*. Use the CMA-ES package for Scilab (it works only for version 5.5 of Scilab) available at <u>https://www.lri.fr/~hansen/cmaes\_inmatlab.html#scilab</u>

Steps:

(a) download the archive (from <u>https://atoms.scilab.org/toolboxes/CMA-ES</u> ) and extract the source files in a local folder

(b) set the local folder as current in Scilab (using Change current directory)

(c) execute builder.sce and loader.sce

(d) instantiate a cmaes object using cma\_new and describe the iterative process which consists of:

(i)construct a new candidate solution (using cma\_ask);

(ii) update the parameters (mainly components of the covariance matrix) to be used during the nest step (using cma\_tell).

#### **Exercise:**

1. Compare the results obtained using CMA-ES with those obtained using the simple evolution strategy in the case of Rosenbrock function (for n=2, 10, 100)

#### 2. Genetic programming

The aim of genetic programming is to design in an evolutionary manner computational structures (arithmetical/logical expressions, classification/decision rules or even programs). In traditional Genetic Programming applications (as *symbolic regression*) the elements of the population are hierarchical structures (e.g. *syntactic trees*). The genetic operators are adjusted to work with such structures. One of the main difficulties in GP is to avoid the proliferation of large structures (the so called *bloat* problem). A possible solution to this problem is to limit the depth of the trees generated during the evolutionary process.

The most popular application of GP is *symbolic regression* aiming to evolve an expression which fits well to some data (unlike the numerical regression which aims to estimate the coefficients of a given model, symbolic regression estimates the model itself).

**Application 3.** Use the "rgp" R package (removed from CRAN 2018) to find an expression which fits a dataset.

Main steps:

- Launch R
- Load package "rgp": Packages ->Load package ... or library("rgp") (if the package is not installed then it should be installed by Packages-> Install package(s)...
- **Define the set of nonterminals** (operators and functions) using functionSet. Example: setNonterminals <- functionSet("+", "\*", "-","/")
- **Define the set of variables using** inputVariableSet.

Example: setVariables <- inputVariableSet("x")</pre>

- **Define the set of constants** using constantFactorySet. Example: setConstants <- constantFactorySet(function() rnorm(1)) (random values generated using the standard normal distribution)
- **Define the test data**: values which will be used to evaluate the approximation accuracy. Example: dateX <- seq(from = -pi, to = pi, by = 0.1)
- **Define the fitness function**: mean square error (measure of the difference between the values of the test function and the values corresponding to the evolved expressions). Example: fitness <- function(f) rmse(f(dateX), sin(dateX)) (if the reference function is sinus)
- **Call the function** corresponding to the evolutionary process (geneticProgramming). Example:

```
geneticProgramming(functionSet = setNonterminals,
inputVariables = setVariables,
constantSet = setConstants,
fitnessFunction = fitness,
stopCondition = makeStepsStopCondition(10000))
```

Particularities of the genetic programming implemented in "rgp":

- The population elements are R expressions (implemented as tree-like structures)
- The population initialization is based on several construction strategies:
  - "grow" (each branch in the tree will be extended until it reaches the maximal length or until a random event occurs)
  - o "full" (all branches in the tree have the maximal length)
  - Combined variant (some elements are generated using the "grow" strategy, others are constructed using the "full" strategy)
- The package implements the traditional crossover and mutation strategies adapted for trees (see slides of lecture 6)
- There are implemented various selection variants using one or several criteria (as in multiobjective optimization). In the multi-criteria variant the aim is to optimize the quality of the result, the simplicity of the elements and the population diversity.

**Exercise 2:** Follow the above steps and test the influence of nonterminals on the quality of the results (by changing the elements of the nonterminals set). Hint: see for instance SymbolicRegression\_GP.r

# **Other resources:**

http://nbviewer.jupyter.org/github/trevorstephens/gplearn/blob/master/doc/gp\_examples.ipynb

# **Homework:**

- **1.** Extend SE.sci by introducing self-adaptation of the parameter s (standard deviation of the normal distribution used in the mutation step see Lecture 5).
- 2. Apply genetic programming (rgp package for R or start from existing Python implementations) to evolve a boolean expression which corresponds to the parity function (the parity function returns 0 if it receives an even number of variables equal to 1 and it returns 1 if it receives an odd number of variables equal to 1). Hint: see rgp\_introduction.pdf